# CATALOGED BY DDC AS AD No. 453421

# 453421

Report No. 4
Fourth Quarterly Report

Covering the Period I April 1964 to 31 August 1964

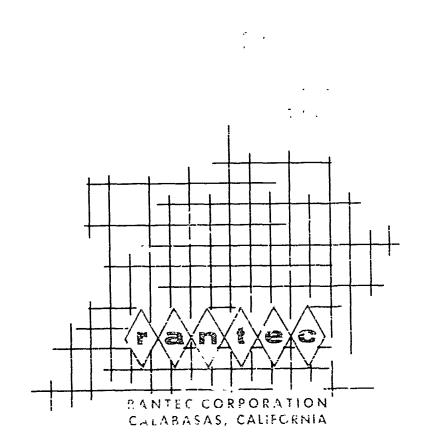
# Investigation of MICROWAVE DIELECTRIC-RESONATOR FILTERS

Prepared for:

U. S. ARMY ELECTRONICS RESEARCH AND DEVELOPMENT LABORATORY FORT MONMOUTH, NEW JERSEY

CONTRACT DA 36-039-AMC-02267(E) TASK NO. 5544-PM-63-91

By: S. B. Cohn and E. N. Torgow



Report No. 4 Fourth Quarterly Report

Covering the Period April 1964 to 31 August 1964

# Investigation of MICROWAVE DIELECTRIC-RESONATOR FILTERS

Prepared for:

U. S. ARMY ELECTRONICS RESEARCH AND DEVFLOPMENT LABORATORY FORT MONMOUTH, NEW JERSEY

CONTRACT DA 36-039-AMC-02267(E) TASK NO 55/4-PM-63-91

By: S. B. Cohn and E. N. Torgow

Rantee Project No. 31625

Approved.

SEYMOUR B COHN, Technical Director

# TABLE OF CONTENTS

SECTION	TĨT <b>LE</b>	PAGĒ
Ĩ	PURPOSÉ	1
IĪ	ABŠTRAČT	2
ШĪ	CONFERENCES AND PUBLICATIONS	4
ΙV	FÄČŤŪAL DAŤA	5
	Introduction	5
	Analysis of Coupling Coefficient - Axial Orientation	6
	Řesonators Óff-Center	17
	Pesonator Tilted from the z Axis	17
	Gombinations of Misalignments	18
	Comparison of Theoretical and Experimental Coupling Coefficients = Axial Orientation	18
	Coupling of Dielectric Resonators to External Lines	ŽZ
	Experimental Investigation of Coupling Techniques	22
	Coupling Between Resonators and Loops	26
v	CÖNCLUSIONS	30
VI	PROGRAM FOR NEXT INTERVAL	37
VII	LIST OF REFERENCES	38
VIII	IDENTIFICATION OF KEY TECHNICAL PERSONNEL	39
	ACTÍA CADOS	40

# LĪST OF ILLUSTRATIONS

FIGURE	TITLE	PAGE
2-1	Dielectric Disk Resonators Axially Oriented in a Square of Rectangular Cut-Off Waveguide	7
2=2	Goordinate System in Rectangular Waveguide Cross Section	13
3-1	Comparison of Theoretical and Experimental Coupling Coefficient Data for Dielectric Disks in the Axial Orientation Waveguide	1 <u>9</u>
4-1	Effect of End Couplings on the Response of a Two-Resonator Filter	2Ž
4-2	Shāpēd Čoupling Loop	Ž4
4-3	Two-Resonator Filter Response with Probe End Couplings	Ž5
4-4	Probe Coupling of Dielectric-Resonator Filter	26
<b>4</b> ÷5	Equivalent Gircuit for Loop	27
4-6	External Coupling Loop	30
4-7	Väriation of Q <sub>ex</sub> with Lateral Displacement of Resonator	34

# SECTION I

# PURPOSE

This program is intended to study the feasibility of high-dielectric-constant materials as resonators in microwave filters, and to obtain dessign information for such filters. Resonator materials shall be selected that have loss tangents capable of yielding unloaded Q values comparable to that of waveguide cavities. The haterials shall have dielectric constants of at least 75 in order that substantial size reductions can be achieved compared to the dimensions of waveguide filters having the same electrical performance.

### SECTION II

### ABSTRACT

An analysis is given of the coupling coefficient between dielectric-disk resonators arranged axially along the center line of a rectangular metal tube below cutoff. As in the case of the transverse orientation of disk axes treated in the Second . . Third Quarterly Reports, a formula is obtained that is reasonably convenient for computation. The formula includes terms for all of the modes excited by the resonators.

In the axial orientation case, t e  $TE_{10}$  and  $TE_{01}$  modes do not contribute to coupling unless the disks at tigned. The lowest order coupling terms are for the  $TE_{20}$  and  $TE_{02}$  modes. Formulas for the  $TE_{10}$  (and  $TE_{01}$ ) coupling terms as a function of transverse and angular misalignments are given. These formulas are useful for determining mechanical positioning tolerances necessary in given filter designs.

Expérimental coupling-coefficient data are given for the axial orientation. Coupling coefficient versus center-to-center spacing was measured for a pair of diéléctric disks in two different sizes of square tubing. Excellent agréément was found with curves computed from the coupling-coefficient formula.

An experimental investigation is described of loop and probe coupling to the end resonators of a series of transverse-oriented coupled dielectric resonators. Principal attention is given in this report to the case of two disks with end couplings adjusted to yield maximally flat response. I dissymmetry of the upper and lower stop bands was observed, and was found to be strongly affected by the end coupling elements. Filter response curves are given for various loop and probe designs, showing large differences in the stop-band behavior. With

one coupling configuration using probes, "infinite" rejection peaks appeared in both stop bands. This effect is attributed to direct probe-to-probe coupling bridging the signal path through the coupled dielectric resonators. A formula is derived for the external Q of a disk resonator coupled to a loop, and approximate experimental agreement is shown.

\* ----

# SECTION III

### CONFERENCES AND PUBLICATIONS

The period of this program has been extended by one year. By mutual agreement of USAERDL and Kantec Corporation, the fourth quarterly report will cover the investigation interval 1 April to 31 August 1964.

On September 30 and October 1, 1964, a conference was held at Rantec Corporation to discuss work completed during the fourth quarter of the program and plans for the second year. Attending the conference were Mr. E. A. Mariani of USAERDL, and Dr. S. B. Cohn and Mr. E. N. Torgow of Rantec Corporation.

Ön September 10, 1964, Dr. S. B. Cohn presented a paper covering some of the work on this program at the International Conference on Microwaves, Circuit Theory, and Information Theory, Tokyo, Japan. The title of the paper was "Recent Developments in Microwave Filters and Related Circuits".

### SECTION IV

### FACTUAL DATA

### 1. Introduction

The First Quarterly Report discusses the nature of dielectric resonators and describes how such resonators may be used in microwave filters. The introduction to that report should be consulted for background information, and for a discussion of problems to be solved before dielectric resonators can be used in practice.

Earlier reports<sup>2,3</sup> on this program have been concerned with dielectric disk reschators in a transverse orientation; that is, with their axes transverse to the axis of the surrounding cut-off waveguide. Another arrangement is that of axial orientation, in which the axes of the resonators and waveguide are co-linear. The axial orientation is interesting because it permits a more compact assembly than transverse orientation. Also, it appears to lend itself to practical assembly techniques, especially when round disks are used in a round waveguide.

An analysis is given of coupling between disks in the axial configuration. The treatment is similar to that for transverse orientation. As in the previous analysis, the coupling coefficient is equal to an infinite series of terms for the various excited modes. In this case, the  ${\rm TE}_{10}$ ,  ${\rm TE}_{01}$ , and  ${\rm TE}_{11}$  modes in rectangular waveguide do not couple to the resonators. The lowest-order coupling modes are the  ${\rm TE}_{20}$  and  ${\rm TE}_{02}$ . The infinite series in the formula for coupling coefficient converges fairly rapidly and is quite convenient for design purposes. In conjunction with this analysis, measurements of coupling coefficient in the axial orientation were made. The agreement between theory and experiment was remarkably good, generally being within 5 percent.

Several two-resonator band-pass filters (transverse orientation) were described in the Third Quarterly Report. The coupling coefficients, as determined from the measured pass-band responses of the filters, agreed closely with the theoretical and experimental values determined earlier. It was noted, however, that the response charactëristics of the dielectric-resonator filters were assymmetric outside of the filter pass bands. The primary source of this assymmetry was ascribed to the characteristics of the input and output coupling elements, which were large, short-circuited loops aligned with their axes parallel to the axes of the dielectric resonators. During the fourth quarter an experimental study was made to determine the factors leading to assymmetric response, and to determine techniques for overcoming this effect. Various loop shapes were investigated, and also probes were used. In addition to achieving improved symmetry, severāl interesting effects were noticed; such as infinite rejection points appearing in the stop bands under certain conditions. This report also gives an analysis of loop coupling to the end resonators of a filter, and approximate correlation with experimental data. The formula, while not exact, is useful for filter design applications.

- 4

# 2. Analysis of Coupling Coefficient - Axial Orientation

In the Second and Third Quarterly Reports a formula was derived for the coupling coefficient between resonant dielectric disks spaced along the center line of a waveguide for the case of the disk axes in the transverse x direction. Another important case is that of the disk axes in the longitudinal z direction; that is, the axes of the disks and waveguide co-linear, as shown in Figure 2-1. An analysis of this axial configuration in rectangular waveguide is given below, and computed coupling-coefficient values are shown to agree very well with measured points. The case of axial configuration in circular waveguide will be treated in the next report.

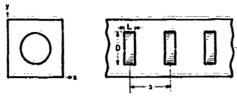


Figure 2-1. Dielectric Disk Resonators Axially Oriented in a Square or Rectangular Cut-Off Waveguide

In the Second Quarterly Report, the following general formula is derived for the coupling coefficient between a pair of identical resonant magnetic dipoles in either a parallel or co-linear configuration:

$$\dot{x} = \frac{\mu_0 H_2 \cdot \dot{m}_1}{2W_{m1}} \tag{2-1}$$

where m<sub>1</sub> and W<sub>m1</sub> are the magnetic dipole moment and stored energy, respectively, of the first dipole when energized at its resonant frequency, and H<sub>2</sub> is the magnetic field at the second dipole due to the first dipole. As discussed previously, the external field of a disk-shaped dielectric resonator (D/L>1) in its lowest-order mode of resonance resembles that of a magnetic dipole directed along the axis of the disk. Thus Eq. Z-1 may be used to compute the coupling coefficient between such resonators.

The analysis will apply to resonators located at any point x, y in the wall guide cross section, but will be a criticularized for the center-line case (x = a/2, y - b/2). For axial orientation,  $m_1$  is in the z-direction. Therefore, the component of  $H_2$  yielding compling is  $H_{2z}$ . Only  $T\dot{E}_{mn}$  modes contribute to coupling, since  $H_z=0$  by definition for  $TM_{min}$  modes.

The Second Quarterly Report  $^2$  gives formulas for the normalized magnetic field components  $h_{xmn}$  and  $h_{y,nn}$  of the  $TE_{min}$  normalized corresponding  $h_{zmn}$  component is

$$h_{zmn} : \frac{2\pi}{\sqrt{con}} \left( \frac{cmn^{\frac{1}{2}}}{Jsb\pi \eta z_{mn}} \right)^{1/2} \cos \left( \frac{m\pi x}{a} \right) \cos \left( \frac{n\pi y}{b} \right) \qquad (2-2)$$

where 5 mi is defined as follows

The other symbols in Eq. 2-2 are defined on pages 9 and 10 of the Second Quarterly Report.

The total field  $H_{2\dot{z}}$  at the second magnetic dipole is expressed in terms of the normalized  $h_{\dot{m}n}$  components as follows (see Second Quarterly Report, page 29)

$$H_{2\dot{z}} = \sum_{\dot{m},n} a_{\dot{m}\dot{n}} h_{\dot{z}\dot{m}\dot{n}} \dot{e}^{-\dot{\alpha}\dot{m}\dot{n}\dot{s}}$$
 (2-3)

where a mn are amplitude factors related to the moment of the first magnetic dipole located at z = 0. Equations 3-43 and 3-38 of the / Second Quarterly Report give

$$a_{mn} = \frac{j\omega\mu_{o}}{2} h_{zmn} \tilde{m}_{1z} \qquad (2-4)$$

It is immediately apparent from Eq. 2-2 that only  $TE_{mn}$  modes of even orders contribute to  $H_2$  at x=a/2 and y=b/2. Thus, the significant orders are m, n=2,0;0,2;2,2;4,0;0,4;4,2;2,4;4,4; etc. In the general case of arbitrary location of the resonator in the cross section,  $TE_{min}$  modes of all orders would be significant.

Equations 2-1 and 2-4 assume  $\dot{m}_1$  to be concentrated at a point. However, in the dielectric resonator,  $\dot{m}_1$  is actually distributed over

the volume of the disk. Inspection of Eq. 2-2 shows that  $h_{2mn}$  has a considerable variation in the plane of the disk, as a result of the cos ( $m\pi x/a$ ) cos ( $m\pi y/b$ ) factor, especially for the higher modes. Thus, Eqs. 2-1 and 2-4 should be rewritten in this manner,

$$k = \frac{\mu_0}{2W_{\tilde{m}\tilde{l}}} \sum_{\tilde{m},n} \hat{a}_{\tilde{m}n} e^{-\tilde{\alpha}_{\tilde{m}\tilde{n}}\tilde{s}} \iiint h_{\tilde{z}\tilde{m}\tilde{n}}(x,y) e^{-\tilde{\alpha}_{\tilde{m}\tilde{n}}\tilde{z}} \tilde{m}_{\tilde{l}z}'' dv \qquad (2-\tilde{s})$$

$$a_{mn} = \frac{j_{\omega \mu}}{2} \iiint h_{zmn}(x, y) e^{-\alpha_{mn}z} \dot{m}_{1z}'' dv$$
 (2=6)

where  $\dot{m}_{1z}^{n}$  is the z component of the volume density of magnetic dipole moment, and integration is performed over the disk area and the axial length, z = -L/2 to L/2. Note that

$$m_{1\tilde{z}} = \iiint m_{1z}^{n} dv$$

When Eqs. 2-5 and 2-6 are combined, one obtains

$$k = \frac{j\omega\mu_0^2}{4W_{m1}} \sum_{m,n} e^{-\tilde{\alpha}_{mn}s} \left[ \iiint h_{zmn}(x,y) e^{-\tilde{\alpha}_{mn}z} \tilde{m}_{1z}^n dv \right]^2 \qquad (2-7)$$

Now consider the fact that  $\tilde{m}_{1z}^u$  is a symmetrical function of z about the central plane of the disk. Also note that  $e^{-c_{mn}z}$  is approximately linear in the z=-L/2 to L/2 range, when L is small. Hence the volume integral may be replaced by the following surface integral over the central plane of the disk

$$\iint h_{\mathbf{z}\hat{\mathbf{n}}i\hat{\mathbf{n}}}(\mathbf{x},y) \; m_{1\hat{\mathbf{z}}}^{\dagger} \; dS$$

where the area density  $m_{1z}'$  is related to  $m_1$  by  $m_1 = \iint m_{1z}' dS$ . Thus

$$k = \frac{j\omega\mu_{\tilde{0}}^{2}}{4W_{\tilde{m}\tilde{1}}} \sum_{m_{\tilde{n}}\tilde{n}} e^{-c_{\tilde{m}\tilde{n}}\tilde{s}} \left[ \iint h_{z\tilde{m}\tilde{n}}(\tilde{x},y) \tilde{m}_{\tilde{1}\tilde{z}}^{\dagger} d\tilde{S} \right]^{2}$$
 (2-8)

This may be written as

$$k = \frac{j_{\omega \mu} \frac{2_{m_1}^2}{4W_{m_1}^2}}{\frac{1}{4W_{m_1}^2}} \sum_{n} (h_{2m_1}^2)^2 K_{m_1} e^{-h_{m_1}^2}$$
 (2-9)

where  $h_{\underline{z}\underline{m}\underline{n}}$  is evaluated at the center of the disk, and  $K_{\underline{m}\underline{n}}$  is defined as follows:

$$K_{\min} = \left[ \frac{\iint h_{z\min}(x,y) m_{1z}^{i} dS}{h_{z\min} \iint m_{1z}^{i} dS} \right]^{2}$$

$$= \left[ \frac{\iint h_{z\min}(x,y) m_{1z}^{i} dS}{h_{z\min}^{i} m_{1}^{i}} \right]^{2}$$
(2-11)

Substitute Eq. 2-2 in Eq. 2-9

$$k = \begin{pmatrix} \mu_0 \dot{m}_1^2 \\ 2W_{m1} \end{pmatrix} \begin{pmatrix} 4\bar{\pi}^2 \\ \bar{a}b \end{pmatrix} \sum_{m,n} \frac{\delta_{mn} \dot{K}_{mn} e^{-c_{mn}\bar{s}}}{\lambda_{cmn}^2 \sigma_{mn}} \cos^2\left(\frac{m\pi x}{\bar{a}}\right) \cos^2\left(\frac{n\pi y}{\bar{b}}\right)$$

$$(2-12)$$

The summation is over  $m=0, 2, 4, 6, \cdots$  and  $n=0, 2, 4, 6, \cdots$ , but does not include the simultaneous combination m=0, n=0, since the  $T\bar{E}_{00}$  mode does not exist in a metal-walled waveguide.

The first factor in Eq. 2-12,  $\mu_0 m_1^{-2}/2W_{\tilde{m}1}$ , is a function only of the geometry of the dielectric resonator and its  $\epsilon_r$  value. It is evaluated in the Second Quarterly Report, pages 31 to 33, for the case of the fundamental mode in a disk (D/L > 1). To a good approximation,

$$k = \frac{j\omega\mu_{0}^{2}}{4W_{m1}} \sum_{m,n} e^{-c_{mn}^{2}} \left\{ \iint h_{zmn}(x,y) m_{1z}^{2} dS \right\}^{2}$$
 (2-8)

This may be written as

$$k = \frac{j\omega \mu_0^2 m_1^2}{4W_{m1}} \sum_{i} (h_{zmn})^2 K_{mn} e^{-\alpha_{mn}^2 s}$$
 (2-9)

where h zmn is evaluated at the center of the disk, and K mn is defined as follows:

$$K_{\min} = \begin{bmatrix} \iint h_{zmn}(x, y) m'_{1z} dS \\ h_{zmn} \iint m'_{1z} dS \end{bmatrix}^{2}$$

$$= \begin{bmatrix} \iint h_{zmn}(x, y) m'_{1z} dS \\ h_{zmn}m_{1} \end{bmatrix}^{2}$$
(2-11)

Substitute Eq. 2-2 in Eq. 2-9

$$k = \begin{pmatrix} \mu_{0} m_{1}^{2} \\ 2W_{m1} \end{pmatrix} \begin{pmatrix} \frac{4\pi^{2}}{ab} \end{pmatrix} \sum_{m,n} \frac{\delta_{mn} K_{mn} e^{-\alpha_{mn} s}}{\lambda_{cmn}^{2} \alpha_{mn}} \cos^{2}\left(\frac{m\pi x}{a}\right) \cos^{2}\left(\frac{n\pi y}{b}\right)$$
(2-12)

The summation is over m=0, 2, 4, 6,  $\cdots$  and n=0, 2, 4, 6,  $\cdots$ , but does not include the simultaneous combination m=0, n=0, since the  $TE_{00}$  mode does not exist in a metal-walled waveguide.

The first factor in Eq. 2-12,  $\mu_0 m_1^{-2}/2W_{ml}$ , is a function only of the geometry of the dielectric resonator and its  $\varepsilon_r$  value. It is evaluated in the Second Quarterly Report, pages 31 to 33, for the case of the fundamental mode in a disk (D/L > 1). To a good approximation,

$$\frac{\mu_{0}\dot{m}_{1}^{2}}{2W_{\dot{m}1}} = \frac{0.927\dot{D}^{4}Lc_{\dot{r}}}{\lambda_{\dot{0}}^{2}}, \ 0.25 \leq L/D \leq 0.7$$
 (2-13)

This is within #2% of a more complicated formula for  $\mu_0 m_1^{-2}/2W_{m1}$ , which also is derived in the Second Quarterly Report. Figure 3-5 of the Second Quarterly Report gives a plot of the error versus L/D, which may be applied to Eq. 2-13 as a correction factor, if desired.

Equation 2-12 will now be particularized for the case of disks located on the central axis of a square waveguide. Thus b = a,  $\dot{x} = \dot{y} = a/2$ , and terms of the summation for m,n and n,m are equal. (For example, the  $T\bar{E}_{20}$  and  $T\bar{E}_{02}$  modes yield equal terms.) Remembering the definition of  $\delta_{mn}$ , we may rewrite Eq. 2-12 as follows.

$$k = \left(\frac{\mu_{0} m_{1}^{2}}{2W_{m1}}\right) \left(\frac{8\pi^{2}}{a\delta}\right) \left\{ \sum_{\substack{\tilde{m}0\\\tilde{a}\tilde{n}d\\\tilde{m}\tilde{m}}} \frac{K_{\tilde{m}\tilde{n}}e^{-0_{\tilde{m}\tilde{n}}\tilde{s}}}{\lambda_{\tilde{c}\tilde{m}\tilde{n}}^{2}\sigma_{\tilde{m}\tilde{n}}} + 2\sum_{\substack{\tilde{m}\tilde{n}\\\tilde{m}\tilde{n}}} \frac{K_{\tilde{m}\tilde{n}}e^{-m\tilde{n}\tilde{s}}}{\lambda_{\tilde{c}\tilde{m}\tilde{n}}^{2}\sigma_{\tilde{m}\tilde{n}}} \right\}$$
(2-14)

m,n = 0, 2, 4, 6, 8, . . .

Equation 2-10 for  $K_{mn}$  will now be evaluated. Since  $m_{12}^{\prime}$  occurs to the same power in both the numerator and denominator, only a relative value is needed. The magnetic dipole moment per unit area is proportional to the magnetic flux per unit area in the central plane of the disk. That is,

$$m'_{lz} \propto B_{l\bar{z}} \propto H_{l\bar{z}}$$

The field distribution in the dielectric disk will be assumed to be that of the second-order solution treated in the First Quarterly Report.

Tnus

$$\bar{m}_{1z} \approx H_{1\bar{z}} \approx \bar{J}_{0} \left(\frac{2\bar{p}_{01}\bar{r}}{\bar{D}}\right), \ r \approx 0 \ t\bar{o} \ \bar{D}/2$$
 (2-15)

where  $p_{\hat{0}\hat{1}}=2.405$  for the fundamental circular-electric mode. Note that  $H_{1\bar{z}}\approx 0$  on the circumference of the disk, as is required by the magnetic-wall cylindrical boundary used in the second-order solution.

Substitute Eqs.  $\hat{Z}$ = $\hat{Z}$  and  $\hat{Z}$ =15 in Eq.  $\hat{Z}$ =10, with h zmn evaluated at the center of the cross section.

$$K_{mn} = \left[ \frac{\iint \dot{cos}\left(\frac{\dot{m}\dot{m}\dot{x}}{a}\right) \, \dot{cos}\left(\frac{\dot{n}\dot{m}\dot{y}}{b}\right) \, J_{o}\left(\frac{2p_{01}\dot{r}}{D}\right) \, r \, dr \, d\theta}{\iint \dot{J}_{o}\left(\frac{2p_{01}\dot{r}}{D}\right) \, \dot{r} \, dr \, d\theta} \right]^{2}$$
(2-16)

m,n = 0, 2, 4, 6, ...

The integral in the denominator will be evaluated first.

$$I_{\hat{D}} = \int_{0}^{2\pi} \int_{0}^{\hat{D}/\hat{Z}} \hat{J}_{\hat{o}} \left( \frac{2\hat{p}_{\hat{0}\hat{1}}\mathbf{r}}{D} \right) \mathbf{r} \, d\mathbf{r} \, d\theta = 2\pi \int_{0}^{\hat{D}/\hat{Z}} \hat{J}_{\hat{o}} \left( \frac{2\hat{p}_{\hat{0}\hat{1}}\mathbf{r}}{D} \right) \mathbf{r} \, d\hat{\mathbf{r}}$$

$$= \frac{\pi \hat{D}^{\hat{Z}}}{2\hat{p}_{\hat{0}\hat{1}}} \hat{J}_{\hat{1}}(\hat{p}_{\hat{0}\hat{1}}) \qquad (2-17)$$

where use was made of 4

$$\int u J_{0}(u) du = u J_{1}(u)$$
 (2-18)

The integral in the numerator will now be treated. As shown in Figure 2-2, the coordinates x and y are related to r and  $\theta$  by



Figure 2-2. Coordinate System in Rectangular Wavegulde Cross Section

$$\dot{x} = \frac{\dot{a}}{2} + r \dot{c} \dot{o} \dot{s} \dot{\theta}$$

$$(\ddot{2} - 1\dot{9})$$

$$\dot{y} = \frac{\dot{b}}{2} + \dot{r} \sin \dot{\theta}$$

Then, because m and n = 0, 2, 4,...

$$\cos\frac{m\pi x}{a}\cos\frac{n\pi y}{b}=(-1)^{(m+n)/2}\cos\left(\frac{m\pi r\cos\theta}{a}\right)\cos\left(\frac{n\pi r\sin\theta}{b}\right)$$
(2-20)

The factor  $(-1)^{(m+n)/2} = \pm i$  can be ignored, since the integral is squared in Eq. 2-16. Thus the numerator integral may be written

$$I_{n} = \int_{0}^{2\pi} \int_{0}^{2\pi} \cos\left(\frac{m\pi r \cos\theta}{a}\right) \cos\left(\frac{n\pi r \sin\theta}{b}\right) J_{o}\left(\frac{2p_{01}r}{D}\right) r dr d\theta$$

$$= \int_{0}^{2\pi} \left(\int_{0}^{2\pi} \cos\left(\frac{m\pi r \cos\theta}{a}\right) \cos\left(\frac{n\pi r \sin\theta}{b}\right) d\theta\right) J_{o}\left(\frac{2p_{01}r}{D}\right) r dr$$

$$= \int_{0}^{2\pi} \left(\int_{0}^{2\pi} \cos\left(\frac{m\pi r \cos\theta}{a}\right) \cos\left(\frac{n\pi r \sin\theta}{b}\right) d\theta\right) J_{o}\left(\frac{2p_{01}r}{D}\right) r dr$$

The inner integration can be performed with respect to 6 by means of the following formula

$$\int_{0}^{\pi} \cos (u \sin \theta) d\theta = \pi J_{o}(u) \qquad (2-23)$$

First, however, certain substitutions are necessary. Because of the following identity

$$\cos A \cos B = \frac{1}{2} (\cos (A + B) + \cos (A - B))$$
 (2-24)

we may write

$$\cos\left(\frac{\tilde{m}\pi\tilde{r}\cdot\tilde{c}\tilde{o}\tilde{s}\cdot\tilde{\theta}}{a}\right)\tilde{c}\tilde{o}\tilde{s}\left(\frac{\tilde{n}\pi\tilde{r}\cdot\tilde{s}\tilde{i}\tilde{n}\cdot\theta}{b}\right)$$

$$=\frac{1}{2}\cdot\cos\left[\tilde{\pi}\tilde{r}\left(\frac{\tilde{m}\cdot\tilde{c}\tilde{o}\tilde{s}\cdot\tilde{\theta}}{a}+\frac{\tilde{n}\cdot\tilde{s}\tilde{i}\tilde{n}\cdot\theta}{b}\right)\right]+\frac{1}{2}\cdot\tilde{c}\tilde{o}\tilde{s}\left[\tilde{\pi}\tilde{r}\left(\frac{\tilde{m}\cdot\tilde{c}\tilde{o}\tilde{s}\cdot\theta}{a}-\frac{\tilde{n}\cdot\tilde{s}\tilde{i}\tilde{n}\cdot\tilde{\theta}}{b}\right)\right]$$

$$(2-25)$$

Now let

$$\frac{m \cos \theta}{a} \pm \frac{n \sin \theta}{b} = C \sin (\theta \pm c)$$

$$= C \sin c \cos \theta \pm C \cos c \sin \theta \qquad (2-26)$$

Therefore

$$\frac{\dot{m}}{a} = \tilde{C} \sin c$$

$$\frac{n}{b} = C \cos c$$

and

$$C = \sqrt{\left(\frac{m}{a}\right)^2 + \left(\frac{n}{b}\right)^2} = \frac{2}{c_{mn}}$$
 (2-27)

Aiso let

$$\theta' = \theta + \hat{c}, d\hat{\theta}' = d\hat{\theta}$$

$$(2-28)$$
 $\hat{\theta}'' = \theta - c, d\theta'' = d\theta$ 

The inner integral of Eq. 2-22 can now be given as

$$\tilde{I}_{\tilde{I}} = \frac{1}{2} \int_{\tilde{C}}^{2\pi + \tilde{C}} \cos \left( \frac{2\pi r}{\lambda_{\tilde{C}m\tilde{n}}} \sin \theta' \right) d\tilde{\theta}' + \frac{1}{2} \int_{-\tilde{C}}^{2\pi - \tilde{C}} \tilde{\cos} \left( \frac{2\pi r}{\lambda_{\tilde{C}\tilde{m}\tilde{n}}} \sin \theta'' \right) d\theta''$$

$$(2-29)$$

These two integrals are equal, since the range of integration in each case is  $2\pi$ , or one period. Therefore, the inner integral of Eq. 2-22 is equal to

$$I_{\tilde{I}} = \int_{0}^{2\pi} \cos\left(\frac{2\pi r}{\lambda_{cmn}} \sin \theta\right) d\theta \qquad (2-30)$$

Equation 2-23 can now be applied, recognizing that  $\int_{0}^{\pi} = \int_{0}^{2\pi}$ . The inner integral is thus equal to

$$I_{\tilde{I}} = 2\pi J_{\tilde{O}} \left( \frac{\tilde{Z}\tilde{\pi}\tilde{r}}{\lambda_{\tilde{C}\tilde{m}\tilde{n}}} \right)$$
 (2-31)

Substitute this in Eq. 2-22 to obtain the numerator integral in the following form:

$$\hat{I}_{N} = 2\pi \int_{0}^{\hat{D}/2} \mathbf{r} J_{o} \left( \frac{2\pi \mathbf{r}}{\hat{\lambda}_{cmn}} \right) J_{o} \left( \frac{\hat{z}\hat{p}_{01}\hat{r}}{D} \right) d\hat{\mathbf{r}}$$
 (2-32)

This can be integrated by means of  $^4$ 

$$\int u J_{n}(\hat{a}u) J_{n}(\hat{a}u) du = \frac{\sum u J_{n}(\hat{a}u) J_{n-1}(\hat{a}u) = \frac{\sum u J_{n-1}(\hat{a}u) J_{n}(\hat{a}u)}{\sum 2 - \frac{2}{z^{2}}}$$
(2-33)

Let 
$$u = r$$
,  $n = 0$ ,  $J_{-1} = -J_1$ ,  $\alpha = 2\pi/\sqrt{cmn}$ ,  $\dot{r} = 2p_{01}/D$ , and  $J_0(p_{01}) = 0$ .

Then

$$\hat{I}_{N} = \frac{2\pi \hat{p}_{01} \hat{J}_{o} \left(\frac{\pi \hat{D}}{\hat{\lambda}_{cmn}}\right) \hat{J}_{1}(\hat{p}_{01})}{\left(\frac{\hat{z}p_{01}}{\hat{D}}\right)^{2} - \left(\frac{\hat{z}\pi}{\hat{\lambda}_{cmn}}\right)^{2}}$$
(2-34)

Substitute Eqs. 2-17 and 2-34 into Eq. 2-16 to obtain

$$K_{\text{mn}} = \left[ \frac{J_{\hat{0}}(\pi \bar{D}/\lambda_{\text{cimn}})}{1 - \left(\frac{\pi \bar{D}}{P_{01}\lambda_{\text{cmn}}}\right)^{2}} \right]^{\frac{1}{2}}$$

$$(2-35)$$

where  $p_{01} = 2.405$ .

Finally, coupling-coefficient values may be computed from Eq. 2-14, utilizing Eqs. 2-13, 2-35, and the following:

$$\lambda_{\text{cmn}} = \frac{1}{\sqrt{\left(\frac{m}{2a}\right)^2 + \left(\frac{n}{2b}\right)^2}}$$
 (2-36)

$$\alpha_{\min} = \frac{2\pi}{\lambda_{\min}} \sqrt{1 - \left(\frac{\lambda_{\min}}{\lambda}\right)^2}$$
 (2-37)

În the next section, Eq. 2-14 is used to compute couplingcoefficient-versus-spacing curves for two sets of practical parameters. In each case excellent experimental agreement is found.

Residual TE 10-Mode Coupling

The  $T\hat{E}_{10}$  and  $T\hat{E}_{01}$  coupling terms are zero in Eq. 2-14 only if the resonators are perfectly aligned on the central axis of the

waveguide. Weak coupling by these modes can occur if the resonators are slightly off center, or are tilted with respect to the waveguide axis. For close spacings of the misaligned resonators, the  $TE_{10}$  and  $TE_{01}$  terms will be negligible compared to the higher-order terms in Eq. 2-14, but for wide spacing they will become significant and even predominate, since their attenuation constants are about half that of the  $TE_{20}$  and  $TE_{02}$  modes.

Two cases of misalignment are considered. These will permit evaluation of the tolerances necessary for Eq. 2-14 to be valid.

### a. Resonators Off-Center

Let the resonators be off center by  $x_1$  or  $=\dot{x}_1$ . Then

$$\mathbf{x} = \frac{\hat{\mathbf{a}}}{2} \pm \mathbf{x}_1 \tag{2-38}$$

Equation 2-12 reduces to the following for the m=1, n=0 term. (The distribution factor  $K_{10}$  is assumed equal to 1 for simplicity.)

$$k_{10} = \left(\frac{\mu_{0} m_{1}^{2}}{2W_{m1}}\right) \frac{\pi^{2}}{a^{3}b} \sin^{2}\left(\frac{\pi x_{1}}{a}\right) \frac{e^{-\alpha_{10}s}}{\alpha_{10}}$$
 (2=39)

This expression applies to resonators displaced in the same direction. For small displacements of the resonators in opposite directions, it can be shown that the  $\tilde{T}\tilde{E}_{10}$ -mode coupling is the negative of the value given in Eq. 2-39.

### b. Resonators Tilted from the z Axis

Let the respector axes be at angle of - with respect to the z-axis in the x, z plane. Then

$$m_{1x} = \hat{m}_1 \sin \varphi \qquad (2-40)$$

The  $T\tilde{E}_{10}$  coupling term is obtained as follows from Eq. 2-28 of the Second Quarterly  $\tilde{R}$ eport $^2$ .

$$k_{10} = \pm \left(\frac{\mu_0 m_1^2}{2W_{m1}}\right) \frac{\sin^2 \psi}{ab} \alpha_{10} e^{-\alpha_{10} s}$$
 (2-41)

In this case the + sign applies to tilting in the same direction and the - sign to tilting in opposite directions.

### c. Combinations of Misalignments

Coupling can occur if one resonator is displaced and the other tilted, or if combinations of these misalignments occur. Also, coupling can occur if the displacements and tilts are in other than the x-y plane. Equations 2-39 and 2-41 are sufficient, however, for estimating misalignment effects. Other possible cases will be of the same order of magnitude, and hence will not be treated in detail.

### Comparison of Theoretical and Experimental Coupling Coefficients - Axia. Orientation

Coupling measurements were made on a pair of identical dielectric-disk resonators on two sizes of cut-off square waveguide. The configuration is as shown in Figure 2-1. Parameters of the disks are D = 0.393 inch, L = 0.160 inch, and  $\epsilon_{\rm r}$  = 97.6. The waveguide dimensions are 0.625 inch and 0.995 inch. The measurement technique is as discussed in the Second Quarterly Report, pages 34 - 37, except for the axial orientation in the present case.

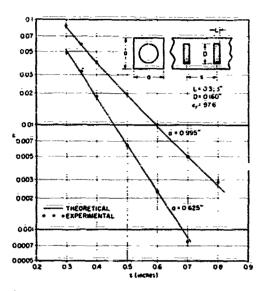


Figure 3-1. Comparison of Theoretical and Experimental Coupling Coefficient Data for Dielectric Disks in the Axial Orientation Waveguide

Figure 3-1 shows theoretical curves and measured couplingcoefficient points plotted versus center-to-center spacing. The theoretical curves are seen to agree with the experimental data extrêmely well. The various measured points are within 5 percent of theoretical, except for two at large spacing that deviate by about 6 to 8 percent. Since these points are for weak coupling, it is likely that the error is due to residual TE13 coupling. This possibility is supported by calculated values at the end of this section.

The curves in Figure 3-1 were computed from Eq. 2-14 with the aid of Eqs. 2-13, 2-35, 2-36, and 2-37. The parameters for the two curves are as follows:

Curve 1	Curve 2		
a = b = 0.625 inch	a - b - 0.995 inch		
$f_o = 3485 \text{ Mc}$	$f_o \approx 3365 \text{ Mc}$		
$\mu_0 m_1^2 / 2W_{m1} = 0.0302$	$\mu_0 m_1^2 / 2 W_{m1} = 0.0281$		

The above  $f_0$  values are measured center frequencies, and are virtually independent of spacing.

In computing the coupling coefficient, significant mode terms are as indicated by x in the tables that follow. Contribution of terms

för other modes amount to less than 0.5 percent of each couplingcoefficient value.

Curve I

Mode	s, inch						
mn	0.3	0.35	0.4	0.5	0.6	0.7	0.8
Ž0 Ž2	×	x	x	×	×	×	×
22	x	x	x	x	x	x	x
40	х	x	x				

Curve II

Mode	s, inch						
mn	0.3	0.35	0.4	0.5	0.6	<u>0.7</u>	0.8
2Ó	x	x	x	×	×	×	x
ŽŽ	x	x	×	x	×	×	x
40	x	x	×	x	x	×	x
42	x	x	x	x	×	×	x
44	x	x	x	x			
60	x	x					
62	x	x					
64	×						

It is clear from these tables that convergence of the infinite series in Eq. 2-14 is rapid except for very close spacing. The more rapid convergence of the series in the case of Curve I results not only from the higher values of the attenuation constants in the smaller waveguide, but also from the fact that  $K_{mn}$  decreases more rapidly with m and n when a given resonator is placed in a smaller waveguide.

Misalignment effects will now be computed to determine the effect of  $TE_{10}$ -mode coupling in the above cases. First assume the resonators to be displaced by  $x_1 = \pm 0.05a$ . By Eq. 2-39,

$$\vec{k}_{10} = \pm 0.00265e^{-2.608}$$
, (a = b = 0.995 inch)

$$k_{10} = \pm 0.0102e^{-4.70s}$$
, (ā = b = 0.625 inch)

At s = 0.8 inch, for example,

$$\hat{k}_{1\hat{0}} = \pm \hat{0}, \hat{0}0\hat{0}3\hat{3}1,$$
  $(\hat{a} = \hat{b} = \hat{0}, \hat{9}\hat{9}\hat{5} \text{ inch})$ 

$$k_{10} = \pm 0.000237$$
, (a = b = 0.625 inch)

Next assume the resonators to be tilted by  $\phi=\pm \hat{5}^{\hat{0}}$ . Equation 2-41 gives

$$k_{10} = \pm 0.000562e^{-2.698}$$
, (a = b = 0.995 inch)

$$k_{10} = \pm 0.00276e^{-4.708}$$
, (a = b = 0.625 inch)

and at s = 0.8 inch,

$$k_{10} \approx \pm 0.0000703$$
,  $(\bar{a} = b = 0.995 inch)$ 

$$k_{10} \approx \pm 0.0000642$$
, (a = b = 0.625 inch)

It is evident from the above examples that the minor discrepancies at the weak-coupling points in Figure 3-1 are explainable in terms of misalignments. An additional factor is possible accentuation of TE<sub>10</sub> mode coupling due to the tuning screw utilized in obtaining synch-ronous tuning of the resonator pair.

# 4. Coupling of Dielectric Resonators to External Lines

# a. Experimental Investigation of Coupling Techniques

The insertion toss response of a two-dielectric-resonator filter, in which the end coupling was accomplished by means of large, short-circuited loops, is shown as Curve I of Figure 4-1. A considerable degree of assymmetry is evident in this curve. Several experiments were conducted during the fourth quarter in order to isolate the cause of the assymmetric response. During the course of these meas-

urements, the distance between resonators was held constant and the input and output couplings were adjusted to yield a maximally flat response.

To determine the degree to which direct coupling between

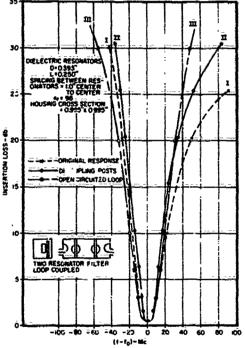


Figure 4-1. Effect of End Couplings on the Response of a Two-Resonator Filter

to which direct coupling between input and output loops affected the response characteristics, two rods were introduced into the filter structure. These rods were located adjacent to each resonator and perpendicular to the plane of the H-field, as shown in Figure 4-1. In this position, the rods have the least effect on the coupling between resonators and on the coupling between each loop and the resonator adjacent to it. Therefore, differences in the filter charac-

teristics observed when the decoupling posts are introduced can be ascribed primarily to the reduction in coupling between the input and output loops. Curve II of Figure 4-1 shows the band pass response of the two resonator filters with the decoupling posts added. A slight narrowing of the pass band was observed, indicating that the posts did have a slight effect upon the coupling between resonators. However, it is evident that the assymmetry was reduced. A third set of data was taken with the decoupling posts removed, but with the loops terminated in an open circuit. The resulting band-pass characteristic, Curve III of Figure 4-1, again exhibited an assymmetry, but the assymmetry is reversed from that observed when the loops were short-circuited. Thus, it appears that in addition to direct coupling, the transmission line effects and the reactances associated with large loops are significant sources of the assymmetries. The effect of these parameters will be examined in greater detail in the following sections.

In addition to the use of a single large loop as a coupling element between a dielectric resonator and its terminating line, several other coupling elements were investigated. A single open-circuited wire parallel to the resonator axis and a small short-circuited wire loop whose axis was perpendicular to the axis of the resonator were placed cause to the resonator. The absence of any detectable coupling verified that there were so significant field components orthogonal to the assumed resonator fields. Measurements of the coupling of multi-turn loops (with loop axis parallel to resonator axis) indicated that a two-turn loop coupled slightly more strongly to the resonator than a single-turn loop, but a three-turn loop of approximately the same diameter coupled more weakly to the resonator. It was deduced that the increase in the loop (see Para b).

A single-turn loop with the plane of the loop parallel to and partially overlapping the flat surface of a resonator was more

weakly coupled to the reschator than was a non-overlapping loop. This results from the fact that, in the former case, some lines of flux lie completely inside the loop and, therefore, do not contribute to the coupling. More lines of flux will link a loop that is tangent to the cylindrical face of the resonator. Thus, it was observed that partially shaping the loop so that it was in contact with the resonator over a section of the cylinder (see Figure 4-2) increased the coupling. All of the loops

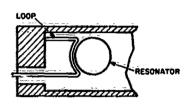


Figure 4-2. Shaped Coupling Loop

nsed in these experiments were constructed with 0.040 to 0.060 inch diameter wire. Therefore, the reactance of the loops was fairly high. The degree of coupling obtained was fairly weak and indicated that these loops were primarily suited to narrow-band-filter coupling elements.

Simple probe coupling was found to be comparable to loop coupling. A simple wire probe bent to be parallel to the electric field lines in a resonator produced a measured value of external Q of approximately 3000 at a probe-to-resonator center spacing of approximately 0.3 inch. A two resonator filter was constructed with probe end couplings. The performance characteristics of this filter are shown in Figure 4-3. Curve I was obtained when both probes were directed toward the same side of the waveguide axis. When one of the probes was reversed so that the probes were on opposite sides of the waveguide axis, the performance shown by Curve II was obtained. The relative positions of the probes and resonators is shown in Figure 4-4. The difference between the two curves is a direct result of the phase relationship between a signal passing through the filter and a signal coupled directly between the probes. For an even number of resonators, it can be shown that the same phase relationship exists between

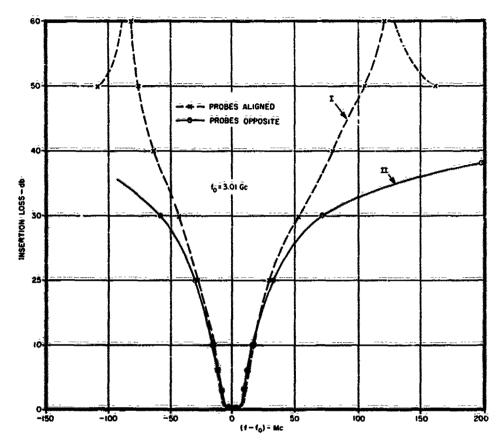
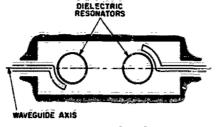
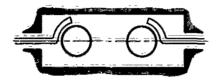


Figure 4-3. Two-Resonator Filter Response with Probe End Couplings

input and output signals above and below the filter pass band. Therefore, probes aligned so that the direct-coupled signal is out of phase with the signal passing through the filter will produce rejection peaks on each side of the pass band. If the orientation of one probe is reversed with respect to the other, the direct-coupled signal is in phase with the filtered signal. In this case, the out-of-band attenuation is reduced on both sides of the pass band. For filters having an odd number of resonators, the phase between input and output signals at frequencies above the pass band differs by 180° from the phase at



(a) PROBES ON OPPOSITE SIDES OF AXIS



(b) PROBES ON SAME SIDE OF AXIS

Figure 4-4. Probe Coupling of Dielectric-Resonator Filter

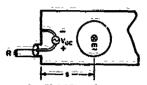
frequencies below the pass band. In this case, probe-to-probe coupling will cause the rejection to be increased en one side of the pass band and decreased on the other side. The relative orientation of the coupling elements will determine on which side of the pass band the peak will occur. Of course, as the number of resonators is increased the spacing between coupling elements also increases and the direct coupling decreases. Therefore, the amount by which the out-of-band rejection is affected by direct coupling decreases, and the partial cancella-

tion ör reinforcement of the rejection characteristic occurs at higher insertion loss levels.

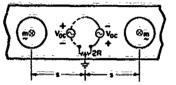
### b. Coupling Between Resonators and Loops

Formulas have been derived for the coupling coefficient between adjacent dielectric resonators inside a waveguide beyond cutoff. The case of cylindrical resonators in rectangular waveguide,
where the axes of the resonators are parallel to each other and normal
to the axis of the waveguide, was treated in the Second and Third Quarterly Reports. Elsewhere in this report the coupling coefficient between
resonators whose axes are aligned with the waveguide axis is derived.
The resonant frequency and unloaded Q of dielectric resonators can be
readily determined from the dimensions of the resonator and its material properties. Data have also been given for the effects of side walls

upon these parameters. Thus, only one factor remains to be determined, the coupling of the end resonators to the terminating lines, in order to completely specify a dielectric resonator filter.



(a) DIELECTRIC RESONATOR AND COUPLING LOOP



(b) DIELECTRIC RESONATOR AND COUPLING LOOP WITH IMAGES



(c) EQUIVALENT CIRCUIT FOR LOOP

Figure 4-5. Équivalent Circuit for Loop

În the preceding subsections, several different techniques for end coupling dielectric resonators to coaxial lines were described. A formula for loop coupling to a dielectric resonator inside a cut-off rectangular waveguide, and with the resonator axis normal to the waveguide axis, has been derived.

A dielectric resonator loop coupled to a terminating line is shown in Figure 4-5a. If it is assumed that the resonator is energized at its resonant frequency  $f_{\dot{\alpha}}$  with a magnetic dipole moment  $m_1$  directed out of the page, the

effect of the wall can be détérmined by taking into account the images of the resonator and loor as shown in Figure 4-5b. The peak open circuited voltage induced in the loop is then given by:

$$2 V_{oc} - 2 \iint_{A} \frac{d\tilde{B}}{dt} \cdot d\tilde{a}$$

$$2 V_{oc} - j\omega\mu_{o} \iint_{A} \tilde{H} \cdot d\tilde{a} = j\omega\mu_{d}H_{2}A$$

$$(4-1)$$

Where  $H_2$  is the mean value of H normal to the loop due to the dipole moment  $m_1$  at a distance s, and A is the area of the loop of Figure 4-55 (twice the area enclosed by the actual loop).

If, as a first approximation, loose coupling is assumed so that the impedance of the resonator seen by the loop at resonance is small and the power dissipated in the resonator can be neglected, then the external Q can be defined by the relation:

$$\hat{\mathbf{Q}}_{\hat{\mathbf{e}}\mathbf{x}} = \frac{\omega \hat{\mathbf{W}}_{\mathbf{m}1}}{\hat{\mathbf{P}}_{\hat{\mathbf{d}}}} \tag{4-2}$$

where  $W_{\hat{m}1}$  is the stored energy in the resonator energized by  $m_1$ , and  $\dot{P}_d$  is the energy dissipated in the external circuit. Representing the loop and external terminations by a series circuit, Figure 4-5c:

$$P_{d} = \frac{1}{2} I^{2} R = \frac{1}{2} \left| \frac{V_{0\dot{c}}}{R + j\dot{X}} \right|^{2} \dot{R}$$
 (4-3)

where R and X are the real and imaginary parts of the impedance seen at the terminals of the induced voltage generator. The factor of 1/2 reduces the open directed peak voltage to its RMS value.

Then

$$\dot{Q}_{ex} = \frac{\ddot{z}\omega \dot{W}_{m1} \left(R^2 + x^2\right)}{\omega^2 \mu_o^2 H_2^2 A^2 \dot{R}}$$

$$= \frac{\dot{z}W_{m1}}{\mu_o \dot{m}_1^2} \cdot \frac{\left(R^2 + \dot{x}^2\right)}{\omega \mu_o \left(H_2 / \dot{m}_1\right)^2 A^2 R}$$
(4-4)

From Eqs. 3-36, 3-52, of the Second Quarterly Report, and Eq. 2-29 of the Third Quarterly Report, the factors:

$$\bar{\mathbf{F}} = \frac{\mu_0 \tilde{\mathbf{m}}_1^2}{2W_{\mathbf{m}1}}$$

$$\bar{\mathbf{k}}(\mathbf{s}) = \frac{\hat{\mathbf{H}}_2}{m_1} \bullet \bar{\mathbf{F}}$$

$$(4-5)$$

can be recognized where F is a factor that depends only upon the parameters of the resonator and

$$F \approx \frac{0.927 \dot{D}^4 L \dot{\epsilon}_{\dot{r}}}{\lambda_0}; \ \dot{0}.25 \leq L/\dot{D} \leq 0.7$$
 (4-6)

för å cylindrical résonator. Furthermore, k(s) is the coupling coefficient between identical résonators, and both experimental and calculated values of k(s) have been given in previous reports for a number of cases.

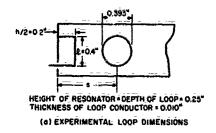
Thus

$$\hat{Q}_{ex} = \frac{\hat{F}}{\left[\hat{K}(s)\right]^2} \cdot \frac{\hat{R}^2 + \hat{X}^2}{\omega \mu \hat{R} A^2}$$
 (4-7)

and as  $\omega_{\sim 0}$  is equal to 2367/ $\lambda$ ,

$$\tilde{Q}_{ex} = \frac{\tilde{F}\lambda (R^2 + X^2)}{2367RA^2 [k(s)]^2}$$
 (4-8)

It can be seen from Eq. 4-2 that the product  $Q_{\rm ex}\left[k(s)\right]^2$  is independent of the spacing between the resonator and the coupling loop. Therefore it would be expected that the experimentally determined values of  $Q_{\rm ex}\left[k(s)\right]^2$  would approach this value for loose coupling,



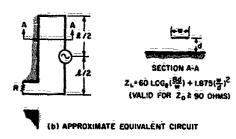


Figure 4-6. External Coupling Loop

when proximity effects are mini-mal. This was confirmed by measurements of  $Q_{ex}$  of the rectangular loop of Figure 4-6a coupled to a cylindrical dielectric resonator in a rectangular waveguide beyond cutoff. The results of these measurements are shown in Table I. A correction factor

$$\frac{1}{Q_{ex}} = \frac{1}{Q_{ex}} = \frac{1}{Q_u} (4-9)$$

was applied to account for the unloaded Q of the resonator alone. The values of  $\left[k(s)\right]^2$  are experimentally determined values as

given in the Second and Third Quarterly Reports. It can be seen that  $\hat{Q}_{ex}[k(s)]^2$  does indeed approach an asymptote for large spacings.

In order to compare the values of  $\hat{Q}_{ex}[k(s)]^2$  of Table I with that a termined by Eq. 4-8, it is necessary that the values of R and X, the real and imaginary parts of the impedance seen by the induced voltage generator be known. Since the fields in the vicinity of the loop are extremely complex, the self inductance cannot be accurately determined. It can be seen from Eq. 4-8 that, if X is comparable in magnitude to, or larger than R, small errors in X can produce large errors in  $\hat{Q}_{ex}$ .

A first approximation assumed that the resistance seen by the voltage generator was the 50-ohm terminating resistance and the reactance was equal to one-half the inductance of a square loop (the actual loop plus its image) in free space.  $Q_{ex}[k(\hat{s})]^2$  computed on this basis was more than twice the asymptotic value given in Table I.

To more accurately account for the presence of conducting walls in the vicinity of the coupling loop, and for the transmission line effects of a long loop, it was then assumed that the loop was a length of transmission line with a voltage generator in series with the line at its center (See Figure 4-66). The line was terminated at one end by a short circuit and at the other end by a 50 ohm resistive load. The characteristic impedance of this line was assumed to be that of a flat thin strip above ground. The length's 1/2 should be corrected to account for the input and terminating lengths of line. A correction factor should also be applied to the characteristic impedance of the flat strip above ground to take into account the stray capacitance between the strip and the side- and top-walls of the cut-off waveguide. There is no direct analytical method for evaluating these correction factors. The dependence of the factor  $\hat{Q}_{ex}[k(\hat{s})]^2$  upon small variations in these parameters can be fairly critical as shown in Table II. The coupling parameter has been computed for a length of I'me 0.2 inch on each side of the voltage generator and for co .ected lengths of 0.25 and 0.3 inch. It can readily be seen that a 0.050 inch variation in length has a significant effect upon the computation of end coupling. Similarly, the last two rows of Table II, which assumed impedance correction factors of  $14^{r_0}$  and  $20^{r_0}$ , demonstrates the critical dependence of the coupling upon the impedance parameter.

The assumption was made in the derivation of Eq. 4-8 that the magnetic field across the loop was constant and equal to the field at the center of the loop (including its image). This approximation is more accurate for a circular loop than for the rectangular loop being considered here. If the actual H field variation for a TE 10 mode in a waveguide beyond cutoff is substituted in Eq. 4-1 the open circuit

TABLE I

Center-to-Center Spacing(s) inch	Q ex meas	Q ex corrected	$\left[k(s)\right]^2$	$Q_{ex}[k(s)]^2$
0.4	85.3	86.3	0.0039	0. 338
.46	130.6	133	. 0024	.314
.50	203	209	.0016	. 334
. 57	355	376	. 00078	. 294
. 63	572	6Žb	.000470	. 29 <del>5</del>
.70	1004-	1181	.000256	.305
.81	1905	2700	.000011	. 296
.97	3933	9940	.00003	. 298

$$\hat{Q}_{ex}_{corrected} = \frac{\frac{1}{Q_{ex}} \frac{1}{Q_{u}}}{\frac{1}{Q_{ex}} \frac{1}{Q_{u}}}$$

 $Q_{\hat{\mathbf{u}}} = 6500$ 

TABLE II

£/2 inch	Z <u>į</u> ohms	Ř ohms	X ohms	$Q_{ex}[k(s)]^2$	$Q_{ex}[k(\hat{s})]^2$ corrected
0.2	114.2	54.8	69.4	0.318	0.254
. 25	114. 2	57	88.5	. 434	.346
.3	114.2	60.5	108	. 564	.451
.3	92.2	59	82	.385	.300
3	100	60	90	. 434	.346

 $f = 3070 \text{ Mc}, \lambda = 3.85 \text{ inches}$ 

voltage determined on the basis of a uniform H field distribution must be corrected by the multiplying factor (sinh ah/2)/(ah/2), where a is the attenuation of the cut-off  $T\bar{E}_{1\bar{0}}$  mode in nepers/unit length and h/2 is the height of the loop above the end wall. For the loop of Figure 4-6, the correction factor reduces  $Q_{\bar{e}\bar{x}}$  by 25%. This correction is shown in the right-hand column of Talle II.

It can be assumed that small displacements of the dielectric resonator with respect to the loop, in a direction transverse to the waveguide axis and perpendicular to the axis of the resonator, would cause very small changes in the magnetic field intensity over the loop area. Furthermore, any change in magnetic field intensity would be symmetrical about the axis of the waveguide. Some effects would be expected as a result of the movement of the equivalent induced voltage generator of Figure 4-65 toward, or away from, the short circuited end of the loop. The variation in Q ex for a lateral displacement of the dielectric resonator was computed for an assumed loop impedance of 100 ôhms and a loop effective lêngth ôf & = 0.6 inch. The measured values of k(s) given in the Second Quarterly Report were used in these calculations. The calculations are compared to measured values in Figure 4-7, for the case of the dielectric resonator tangent to the loop (centerto-center spacing of 0.4 inch). It can be seen that the actual variation in Q is significantly greater than was predicted by the computations. The coupling is considerably weaker when the resonator is displaced toward the input end of the loop and stronger when displaced toward the short-circuited end of the loop.

It can be seen from Figure 4-7, that the stray electric field of a dielectric resonator, energized as shown, produces an electric field between the loop and ground in one direction near the shorted end of the loop and in the opposite direction at the input end of the loop.

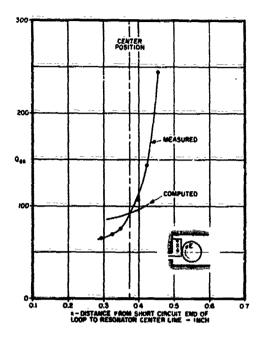


Figure 4-7. Variation of  $Q_{ex}$  with Lateral Displacement of Resonator

When the resonator is centered with respect to the loop, these components of electric field are approximately equal and the coupling is entirely due to the magnetic field in the resonator. It can be deduced from the measured data that the electric coupling tends to increase the coupling when the resonator is positioned near the short circuited end of the loop wh we maximum magnetic field coupling occurs. When the resonator is displaced away from the shorted end of the loop, where the magnetic field coupling is weaker, the electric field coupling tends to counteract the magnetic field coupling resulting in a significant

decrease in the total coupling between loop and resonator.

Thus it has been demonstrated that the coupling between a dielectric resonator and a loop is critically dependent upon the size, shape, and position of the loop, both with respect to the resonator and with respect to the cut-off waveguide housing. From the steepness of the curves for k(s) as a function of s, it can also be seen that small errors in s will produce substantial errors in the value of  $Q_{ex}$ . The error here is greater than in the case of coupling between two resonators, since  $Q_{ex}$  is inversely proportional to  $\left[k(s)\right]^2$ . Thus the design of coupling loops for dielectric resonators must be somewhat empirical. This is entirely analogous to the design of loops in cavity-resonator

filters, where some range of adjustment of loop size or position is generally provided, and the adjustment is made such that the prescribed filter performance is achieved.

Design formulas, such as that given by Eq. 4-8 are valuable in that:

- The approximate size and position of a coupling loop can be determined for a specified degree of coupling; and
- Variations in coupling as a result of changes in the position or shape of a coupling loop can be predicted. It has also been shown that relatively large coupling loops are required for use with dielectric resonators to realize filters exhibiting fairly narrow (up to approximately 2%) bandwidths.

#### SECTION V

#### CONCLUSIONS

The axial arrangement of dielectric disk resonators has several promising properties compared to the previously analyzed transverse arrangement: (1) larger coupling values can be achieved; (2) a given number of resonators can be packed into a smaller volume; and (3) a practical, rugged structure can be readily constructed, especially with circular disks in a cut-off circular waveguide. The coupling-coefficient formula derived for this orientation gives excellent agreement with experimental data.

The problem of loop or probe coupling to the end dielectric resonators of a band-pass filter is too complex for precise analysis. Rough agreement was found between experimental data and a formula for the external Q of an end resonator (transverse orientation) coupled to a loop, but it is clear that empirical adjustment would be necessary in a given filter design. This fact is not unexpected, however, since adjustability of loop or probe couplings is generally necessary in conventional coaxial or waveguide-cavity filters having coaxial terminations. The shape of the stop-band skirts is especially dependent on the nature of the loops or probes. This behavior is partly due to the equivalent circuit of the coupling element and partly due to coupling beyond the adjacent resonator to the second resonator and to the output loop or probe. With probe coupling, "infinite" rejection points could be achieved in both stop bands. This was attributed to a secondary signal path directly between the probes.

#### SECTION VI

#### PROGRAM FOR NEXT INTERVAL

The axial-orientation analysis will be extended to the case of a circular cut-off waveguide surrounding the dielectric disks. An approximate formula will be derived for end-loop coupling for this geometry. Experimental data will be obtained for comparison. Applicability of the axial orientation to medium- and wide-band filters will be investigated.

An experimental and theoretical study will be started on bandrejection-filter configurations.

The study of metal-wall proximity effects on Q and  $f_{_{\rm O}}$  of dielectric resonators will be extended and completed.

#### SECTION VII

#### LIST OF REFERENCES

- 1. S. B. Cohn and C. W. Chandler, "Investigation of Microwave Dielectric-Resonator Filters," First Quarterly Report on Contract DA-36-039-AMC-02267(E), 1 July 1963 to 30 September 1963, Rantec Corp., Project No. 31625.
- 2. S. B. Cohn and K. C. Kelly, "Investigation of Microwave Dielectric-Resonator Filters," Second Quarterly Report on Contract DA-36-039-AMC-02267(E), 1 October 1963 to 31 December 1963, Rantec Corp., Project No. 31625.
- 3. S. B. Cohn and K. C. Kelly, "Investigation of Microwave Dielectric-Resonator Filters," Third Quarterly Report on Contract DA-36-039-AMC-02267(E), 1 January 1964 to 31 March 1964, Rantec Corp., Project No. 31625.
- 4. E. Jahnke and F. Emde, "Tables of Functions with Formulae and Curves," p. 145 and p. 150, Dover Publications, New York, 1943.

## SECTION VIII

# IDENTIFICATION OF KEY TECHNICAL PERSONNE'.

	Hours
Dr. Seymour B. Cohn Specialist	242
Mr. Eugene N. Tórgow Staff Enginear	86
Mr. Charles W. Chandler Senior Engineer	56
Mr. Kenneth C. Kelly Senior Engineer	257
Mr. Richard V. Reed Engineer	513
Mr. Charles M. Oness Enginees	100

AD	ONCLASSIFIED	AD DIV	UNCLASSIFIED
Fantes Corporation, Galabasas, California		Rantec Corporation, Calabasas, California	
AICROWAYE DIELECTRIC-RESON.TOR FILTERS, by 3 B. Chan and E. N. Trigue, an investigation. Four! Guarterly Report.  1. April to 11 August 1964, 645, incl., illus. abbre, 3 refe. [rept. o. 4, pop., 51823] [Cantract DA.16-019-AMC-12201]]  An analysis is given of the coupling coefficient between dielectric-districtions of the army data are served.  Also recently a compared to the coupling coefficient between dielectric-comparison of the army state of a servine gestion of the army state of a serven comparison.  In the axist or compared to the serven served and Third Guarterly Reports, a formula is obtained that is resonably convenient for comparison of the arms are to the TE, and TE, product the lower tribute to coupling terms are to the TE, and TE, product the lower tribute to coupling terms are to the TE, and TE, product the invented for the TE, in the tribute of the TE, and TE, product the trigon of tensures and angular misalignment are given.  Experimental coupling coefficient data are given to the axis of the result size of measured for a pair of dielectric class in two different size of	1. Dielectric-Resonator Filters Analyses I. Title: Microwave Dielectric-Resonator Filters II. Cohn. S. B. and Forgow, E. N. III. hantec Corp., Galabasas, Calif. IV. Contract DA 36-039.	MICROWAVE DIELECTRIC-MESONATOR FILTTRS, by 3. B. Connast E. N. Torgow, an investigation. Fourth Querer's Report. 1-April to 31 Angeril 1964. 405. mel. 1819. asbles, 4 refs. trept. 4-4, proj. 18153 (Contract DA-36-039-AMC-022078) An analysis is given of the coupling coefficient by neeth districted districted and remain the before caucif. As it the rest of the of a rectarges mental shop the restry line of a rectarge reports of the caucification of the sast strated in the Second and Third Charterly Reports, 2 formulas to obtained that its reasonably convenient for the base to obtain a solution to second and Third Charterly Reports, 2 formulas to district the Second and Third Charterly Reports, 2 formulas as better the SEQ and TEQ, modes do not contribute to coupling units as for the TEQ, and TEQ, modes do not contribute to the TEQ, and TEQ, modes as for the text of the tex	1. Dielectric-Resonator Filters Analyses 1. Title: Microwave Dielectric-Resonator Filters III. Cohn. S. B. and Torgow, E. N. III. Rantec Corp., Calabasas, Cailf. IV. Contract DA 36-039- AMC-02267{E}
(over)	UNCLASSIFIED	· (over)	UNCLASSIFIED
AD FIV Rantuc Corporation, Galabasas, California	UNCLASSIFIED	AD DIV Rantec Corporation, Calabasas, California	UNCLASSIFIED
ANGEGOM A.E. DIELECTRICRESONATOR PILTERS. by S. B. Cohm and F. N. Lorgue, an Investigation. Fourth Softertor Report. Dept. to D.I. Acquest 1964, 479. Incl. Illus. Lables, 4 refs. Stept. no. 4 proj. 5.429 (Contract Da.19. AMC.02217E).  An ac. type 10 given of the roughly coefficient between distortic-date remaster acranged analyt along the venter line of a recent guidar metal tone before could. As in the vase of the transverse guidar metal tone before could. As in the vase of the transverse guidar metal tone before could. As in the vase of the transverse computation of disk assa treated in the Second and Dirid Dustrerly Reports. A formula is stained day it reas nably convenient for computation. In the axial orrelation case, the TEgo and TEgo modes do not one transverse to coupling terms are for the TEgo of Left Tego and the lowest modes coupling terms are given for the LE, of lend LE, to coupling rents are given for the axial orrelation. Coupling coefficient varian center-to-center pasting was remained for a paly of dielectric dieks in two different sizes of	1. Dielectric-Resonator Filters Analyses I. Title: Microwave Dielectric-Resonator Filters II. Cohn, S. B. and Torgow, E. N. III. Rantec Corp., Calabasas, Calif. IV. Contract DA 36-039- AMC-02267(E)	MICROWAYE DILLECTRIC-RESONATOR FILTERS, by S. B. C.An and E. M. Torgone and the student of the following the delice ables of Fills.  An analysis to given on the coupling coefficient between delectric delice reconstant arranged smally along the center lives of a recent guide meable in the second to the constant of the resonation of this was treated to the Second and Third Charterity Reports. a formula is obtained that is reasonably convenient for computation.  In the sailst orientation case, the T.E., and T.E., and desired convenient for the sailst orientation of this was treated for the Exceeding Convenient for the sailst orientation and Third Charterity for the T.E., and T.E., and T.E., and T.E. in the sailst orientation are coupling them are to the T.E., and T.E., and T.E. for the T.E., and T.E., and T.E. for the T.E.	1. Dielectric-Resonator Filters Analyses 1. Title: Microwave Dielectric-Resonator Filters 11. C.hn., S. B. and T. rgow, E. N. 111. Panter Corp., Calabasa, Calif. 11V. Contract DA 36-039. AMC-02267(E)
(over)	UNCLASSIFIED	(over)	UNCLASSIFIED

UNCLASSIFIED	Filters  Dielectric-Constant Resonator Cylindrical Rectangular Magnetic-Dipole Magnetic-Dipole Magnetic-Dipole Magnetic-Pipole Magnetic-Pipole Magnetic-Pipole Mode Coupling Cosfficient Store Energy Bandpass Loop Coupling Probe Coupling TiO <sub>2</sub> UNCLASSIFIED	UNITERMS Fiters  UNITERMS Fiters Dielectric-Constant Resonator Cylindrical Recengular Resengular Magnetic-Dipole Magnetic-Dipole Massurement Microwava Mode O Coupling Coefficient Stored Energy Bandgass Lory Coupling Frobe Coupling Tito2 UNCLASSIFEID
Ab	square tobing. Excellent agreement was found with curves compassed from the coupling-coefficient formula.  As apparimental investigation is described of loop and probe coupling to the definition of series of Larawrege-constitution of the coupling to the season for collection of series of Larawreges-constitution of the coupling that caponia. The principal attention is given in this special coupling that caponia. A dissymment with the coupling tablesed to yield the coupling that caponia. A dissymment with the coupling tablesed to yield the coupling tenters. Filter response curver for various loop that one coupling configuration using probes. "Latinty" rejected to dispass appeared in but to to be strongly stiftered to dispass appeared in the loop to the supplied to dispassed to the loop to the supplied to dispassed to the probes. "Latinty" rejected to dispasse appeared in the loop to the state.  The coupled districtive resonators. A for rula is derived for the state.  Innestal agreement is shown.	square tubing. Excellent agreement was found with curve compares from the couplity-coefficient-formula.  An experimental investigation is described to loop and probe coupling to the end resolutors of a saries of transverse-oriented coupling to the end of the case of two datas with end couplings adjusted to yield maximally filt response. A desaymentry of the upper and lower does hand see a coupling afferment. Filter response curve if of various loop and seed coupling afferment. Filter response curve if of various loop with the case of two datas and seed coupling afferment is selected to the case of two bands and speaks appeared to various loop early appeared to be the stoppeared for being the congrete designs show large differences in the slop-band oblavior.  With one coupling configuration using probes, "whitting respection peaks appeared to believe the green of the configuration of a daily resonator. A formula is farjound for the exterimental agreement is shown.
UNC: ASSIFIED	UNITERMS Filter. Dielectric-Constant Resonator Cylindrical Rectangular Magnetic-Dipole Measu ement Microwave Mode Q Coupling Coefficient Stored-Energy Bandges Loop-Goupling TiO2	UNCLASSIFIED  UNITERAIS Filtera Disjectric-Constant Resonator Cylindrical Rectangular Magnetic-Dipola Magnetic-Dipola Magnetic-Dipola Magnetic-Dipola Magnetic-Dipola Magnetic-Dipola Coupling Coefficient Stored Energy Basdpasa Losp Coupling Frobs Coupling TiO <sub>2</sub> UNCLASSIFIED
۸١α	requere habing. Secretaria agreement was found with curves computed from the conjuctific feed formula.  An expert necessary and agreement of the conjuctific formula.  Particle of it not secretaria. Principal attentions in given in this impairment of the appear and one maintainty. The conjugation is given in this impairment of the appear and lower maintainty. The conjugation is given in this stopping that response coupling adjusted to yield the conjugation of the appear and lower the formula desired and was constructed to the appear and lower the conjugation of the appear and lower that appeared in both stop baseds. This effect is uttributed to different an appeared in both stop baseds. This effect is uttributed to different to probe coupling prolificy and is effect in uttributed to different to probe coupling prolificial and the formula is a feet to different to a dish freement is shown.	AD DIV  An experimental investigation is cesswided with curves compand at the coupling conflicts. formula  An experimental investigation is cesswided of loop and probe coupling addition to be est free of the assets of transverse contributed out pled districts, resonators. Frincipal attention is given in this response. A disaymment of the districts of the district of the coupling addition. Better the district of the coupling configuration using pribate and lower and publing configuration using pribate. In any appeared in the supplied to the coupling addition to the district and there is an any all only any and any and the district is strictly at include to the coupling bridging the light pith through the coupling and any of the coupling bridging the algorithm as a significant of the coupling addition to the coupling bridging the again and approximate appeared in the enter of the coupling bridging the significant of the coupling the significant of the

# UNITED STATES ARMY ELECTRÔNICS RESEARCH & DEVELOPMENT LABORATORIES STANDARD DISTRIBUTION LIST RESEARCH AND DEVELOPMENT CONTRACT REPORTS

<u>C</u> .	opies
OASD (R & E), Room 3E1065, ATTN: Technical Library, The Pentagon, Washington 25, D.C.	ì
Chief of Research and Development, OCS, Department of the Army, Washington 25, D. C.	1
Commanding General, U.S. Army Mate. of Command ATTN: R & D Directorate, Washington 25, D.C.	į
Commanding General, U.S. Army Electronics Command ATTN: AMSEL-AD, Fort Monmouth, New Jersey	3
Commander, Defense Documentation Centur, ATTN: TISIA Cameron Station, Building 5, Alexandria, Virginia 22314	21
Commanding Officer, U.S.A. Combat Developments Command ATTN: CDCMR-E, Fort Belvoir, Virginia	1
Commanding Officer, U.S. Army Combat Developments Command Communications-Electronics Agency, Fort Huachuca, Arizona	1
Chief, U.S. Army Security Agency, Arlington Hall Station Arlington 12, Virginia	2
Deputy President, U.S. Army Security Agency Board Arlington Hall Station, Arlington 12, Virginia	l
Commanding Officer, Harry Diamond Laboratories, Connecticut Avenue & Van Ness St., N. W., Washington 25, D. C.	ł
Director, U.S. Naval Research Laboratory, ATTN. Code 2027 Washington 25, D.C.	1
Commanding Officer and Director, U.S. Navy Electronic Laborator, San Diego 52, California	ł
Aeronautical Systems Division, "TTN" ASNAS ( Wright-Patterson Air Force Base, Ohio 45433	ì
Air Force Cambridge 3 search Laboratories, ITA CRZC L.G. Hanscom Field, Bedford, Massachusetts	1
Air Force Cambridge Research Laboratories, .IFN CRNL-R L.G. Hanscom Field, Bedford, Massach setts	Ī

·	<u>Copies</u>
L.G. Hanscom Field, Bedford, Massachusetts	1
Rome Air Development Center, ATTN: RAALD Griffiss Air Force Base, New York	1
Advisory Group on Electron Devices, 346 Broadway, 8th Floor, New York, New York 10013	3
AFSC Scientific/Technical Liaison Öffice, U.S. Naval Air Development Genter, Johnsville, Penneylvania	1
USAEL Liâison Öffice, Rome Air Development Center, ATTN: RAOL, Griffiss Air Force Base, New York	1
NASA Representative (SAK/DL), Scientific and Technical Information Facility, P.O. Box 5700 Bethesda, Maryland 20014	2
Commander, U.S. Army Research Office (Durham) Box CM = Duke Station, Durham, North Carolina	1
Director of Procurement & Production Directorate ATTN: AMSEL-PP-E-ASD-5, Fort Monmouth, New Jersey	1
Commanding Officer, U.S. Army Engineer Research & Development Laboratories, ATTN: STINFO Branch Fort Belvoir, Virginia 22060	2
Marine Corps Liaison Office, U.S. Army Electronics Laboratories, Fort Monmouth, New Jersey	1
AFSC Scientific/ Technical Liaison Office, U.S. Army Electronics Laboratories, Fort Monmouth, New Jersey	1
Commanding Officer, U.S. Army Electronics Laboratories, ATTN: AMSEL/RD-DR/DE, Fort Monmouth, New Jersey	1
Director, U.S. Army Electronics Laboratories, ATTN: Technical Documents Center, Fort Monmouth, New Jersey	1
Commanding Officer, U.S. Army Electronics Laboratories ATTN: AMSEL-RD-ADO-RHA, Fort Monmouth, New Jersey	1
Commanding Officer, U.S. Army Electronics Research & Divelopment Activity, ATTN: SELWS-A	1
White Sands, New Mexico 88002	<u>इ</u> ह

;

## SUPPLEMENTAL DISTRIBUTION

	Copies
National Bureau of Standards, Engineering Electronics Section ATTN: Mr. Gustave Shapiro, Chief, Washington 25, D.C.	1
Chief, Bureau of Ships, Department of the Navy ATTN: Mr. Gumina, Code 68182, Washington 25, D. C	i
Commander, Rome Air Development Center, ATTN: Mr. P. Romanelli (RCLRA-2), Griffiss Air Force Base, New York	1
Elec. Engineering Department, University of California at Santa Barbara, ATTN: Dr. G. Matthaei, Santa Barbara, California	1
Physical Electronic Laboratories, 1185 O'Brien Drive, Menlo Park, California, ATTN: Dr. Carter	1
Stanford Research Institute, Menlo Park, California ATTN: Dr. Young	1
Mr. Robert Standley, Antenna Research Facility I. T. Research Institute, Box 205, Geneva, Illinois	l
Mr. Jesse J. Taub, Airborne It struments Laboratory Deer Park, L.I., New York 11729	l
Professor E. J. Smoke, Rutgers, The State University N. J. Ceramic Research Station, New Brunswick, New Hersey	1
N. J. Gamara, Manager, Antenna R and D Department, L ectronic Defense Laboratory, Sylvania Elec. Prods., Inc., P. 2008 Mountain Jiew. California	1
Director, U.S. Army Electronics Laboratories	
Fort Monmouth, New Jersey	ì
ATIN: AMSEL-RD-PE (Division Director) ATTN: AMSEL-RD-PE (Dr. E. Roth)	1
ATIN: AMSEL-RD-P (Department Director;	1
ATTN: AMSEL-RD-PEM (Mr. N. Lipetz)	1
ATTN: AMSEL-RD-PEM (Mr. J. Charlton)	1
ATTN: AMSEL-RD-PEM (Mr. E. Mariem)	